FOR EDEXCEL

GCE Examinations

Advanced Subsidiary

Core Mathematics C3

Paper I

MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks could be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.



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C3 Paper I – Marking Guide

1.

$= \dfrac{2x}{2x^2+3x-5} \times \dfrac{x^2-x}{x^3}$ M1

$= \dfrac{2x}{(2x+5)(x-1)} \times \dfrac{x(x-1)}{x^3}$ M1 A1

$= \dfrac{2}{x(2x+5)}$ M1 A1 **(5)**

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2. *(a)* $A\ (0, 5),\ B\ (0, e^2)$ B2

$\therefore\ AB = e^2 - 5$ B1

(b) $3 + 2e^x = e^{x+2} = e^2e^x$ M1

$3 = e^x(e^2 - 2)$

$e^x = \dfrac{3}{e^2-2}, \qquad x = \ln \dfrac{3}{e^2-2}$ M1 A1

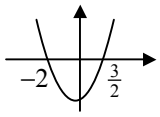
$\therefore\ y = e^2e^x = e^2 \times \dfrac{3}{e^2-2} = \dfrac{3e^2}{e^2-2}$ M1 A1 **(8)**

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3. *(a)* $f'(x) = \dfrac{2x\times(4x+1)-(x^2+3)\times 4}{(4x+1)^2} = \dfrac{4x^2+2x-12}{(4x+1)^2}$ M1 A2

(b) $\dfrac{4x^2+2x-12}{(4x+1)^2} \geq 0$ M1

for $x \neq -\frac{1}{4}$, $(4x+1)^2 > 0$ $\therefore\ 4x^2 + 2x - 12 \geq 0$ M1 A1



$2(2x - 3)(x + 2) \geq 0$ M1

$x \leq -2$ or $x \geq \frac{3}{2}$ A1 **(8)**

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4. *(a)* $\dfrac{dy}{dx} = 2x - 5 + \dfrac{2}{x}$ M1

$x = 3,\ y = -6,\ \text{grad} = \frac{5}{3}$ A1

grad of normal $= -\frac{3}{5}$ M1

$\therefore\ y + 6 = -\frac{3}{5}(x - 3)$ M1

$5y + 30 = -3x + 9$

$3x + 5y + 21 = 0$ A1

(b) SP: $2x - 5 + \dfrac{2}{x} = 0$

$2x^2 - 5x + 2 = 0$ M1

$(2x - 1)(x - 2) = 0$ M1

$x = \frac{1}{2}, 2$ A1 **(8)**

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5. *(a)* $= g(5) = \log_2 16 = 4$ M1 A1

(b) $y = \log_2 (3x + 1)$

$3x + 1 = 2^y$ M1

$x = \frac{1}{3}(2^y - 1)$

$g^{-1}(x) = \frac{1}{3}(2^x - 1)$ M1 A1

(c) $fg^{-1}(x) = f[\frac{1}{3}(2^x - 1)] = 2(2^x - 1) - 1 = 2(2^x) - 3$ M1

$\therefore\ 2(2^x) - 3 = 2$

$2^x = \frac{5}{2}$ A1

$x = \dfrac{\ln \frac{5}{2}}{\ln 2}$ or $\dfrac{\ln 5 - \ln 2}{\ln 2}$ M1 A1 **(9)**

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6. *(a)* $\cos(A+B) \equiv \cos A \cos B - \sin A \sin B$
$\cos(A-B) \equiv \cos A \cos B + \sin A \sin B$
subtracting, $\cos(A+B) - \cos(A-B) \equiv -2 \sin A \sin B$ M1 A1
let $P = A + B$, $Q = A - B$

adding, $P + Q = 2A \Rightarrow A = \frac{P+Q}{2}$ M1

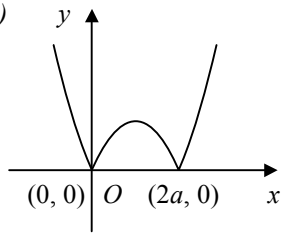
subtracting, $P - Q = 2B \Rightarrow B = \frac{P-Q}{2}$

$\therefore \cos P - \cos Q \equiv -2 \sin \frac{P+Q}{2} \sin \frac{P-Q}{2}$ A1

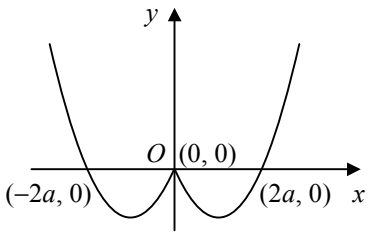
(b) $(\cos 5x - \cos x) + \sin 3x = 0$
$-2 \sin 3x \sin 2x + \sin 3x = 0$ M1
$\sin 3x(1 - 2 \sin 2x) = 0$ M1
$\sin 3x = 0$ or $\sin 2x = \frac{1}{2}$ A1
$3x = 0, 180, 360$ or $2x = 30, 150$ B1
$x = 0, 15, 60, 75, 120$ M1 A2 **(11)**

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7. *(a)* *(i)*



(ii)



B3 B3

(b) $= f(3a^2) = 9a^4 - 6a^3$ M1 A1

(c) $gf(x) = 3a(x^2 - 2ax)$ M1
$\therefore 3a(x^2 - 2ax) = 9a^3$
$x^2 - 2ax - 3a^2 = 0$ A1
$(x + a)(x - 3a) = 0$ M1
$x = -a, 3a$ A1 **(12)**

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8. *(a)* $f(0.7) = -0.25$, $f(0.8) = 0.23$ M1
sign change, $f(x)$ continuous $\therefore$ root A1

(b) $f'(x) = 2 + \cos x + 3 \sin x$ M1
$x = 0$, $y = -3$, grad $= 3$ A1
$\therefore y = 3x - 3$ M1 A1

(c) $\cos x + 3 \sin x = b \cos x \cos c + b \sin x \sin c$
$b \cos c = 1$, $b \sin c = 3$

$\therefore b = \sqrt{1^2 + 3^2} = \sqrt{10}$ M1
$\tan c = 3$, $c = 1.25$ (3sf) M1

$\therefore a = 2$, $b = \sqrt{10}$, $c = 1.25$ A2

(d) SP: $2 + \sqrt{10} \cos(x - 1.249) = 0$

$\cos(x - 1.249) = -\frac{2}{\sqrt{10}}$ M1

$x - 1.249 = \pi - 0.8861, \pi + 0.8861 = 2.256, 4.028$ M1
$x = 3.50, 5.28$ (2dp) A2 **(14)**

Total **(75)**

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Performance Record – C3 Paper I

Question no.	1	2	3	4	5	6	7	8	Total
Topic(s)	rational expressions	exponentials and logarithms	differentiation	differentiation	functions	trigonometry	functions	numerical methods, differentiation, trigonometry	
Marks	5	8	8	8	9	11	12	14	75
Student									

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